

MTH 7 Trigonometry Formula Sheet

Sum and Difference Formulas

$$\sin(u + v) = \sin(u) \cos(v) + \cos(u) \sin(v) \quad \cos(u + v) = \cos(u) \cos(v) - \sin(u) \sin(v)$$

$$\sin(u - v) = \sin(u) \cos(v) - \cos(u) \sin(v) \quad \cos(u - v) = \cos(u) \cos(v) + \sin(u) \sin(v)$$

$$\tan(u + v) = \frac{\tan(u) + \tan(v)}{1 - \tan(u) \tan(v)} \quad \tan(u - v) = \frac{\tan(u) - \tan(v)}{1 + \tan(u) \tan(v)}$$

Double Angle Formulas

$$\sin(2u) = 2 \sin(u) \cos(u) \quad \tan(2u) = \frac{2 \tan(u)}{1 - \tan^2(u)}$$

$$\begin{aligned} \cos(2u) &= \cos^2(u) - \sin^2(u) \\ &= 2 \cos^2(u) - 1 \\ &= 1 - 2 \sin^2(u) \end{aligned}$$

Half Angle Formulas

$$\begin{aligned} \sin\left(\frac{u}{2}\right) &= \pm \sqrt{\frac{1 - \cos(u)}{2}} & \cos\left(\frac{u}{2}\right) &= \pm \sqrt{\frac{1 + \cos(u)}{2}} \\ \tan\left(\frac{u}{2}\right) &= \frac{1 - \cos(u)}{\sin(u)} = \frac{\sin(u)}{1 + \cos(u)} \end{aligned}$$

Power Reducing Formulas

$$\sin^2 u = \frac{1 - \cos 2u}{2} \quad \cos^2 u = \frac{1 + \cos 2u}{2}$$

Polar Coordinate Conversions

$$\begin{aligned} x &= r \cos \theta \\ y &= r \sin \theta \\ x^2 + y^2 &= r^2 \end{aligned}$$

Law of Sines:

$$\frac{\sin(A)}{a} = \frac{\sin(B)}{b} = \frac{\sin(C)}{c}$$

Law of Cosines:

$$c^2 = a^2 + b^2 - 2ab \cos(C)$$